

## Derivatives

If  $y = f(x)$ , then the derivative is defined as

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

### Basic Properties & Formulas

$f(x)$  and  $g(x)$  are differentiable functions (there derivative exists),  $c$  and  $n$  are any real numbers,  $f', g'$  are derivatives of  $f$  and  $g$  with respect to  $x$ .

Equivalent notations for derivative  $f'(x) = y' = \frac{df}{dx} = \frac{dy}{dx} = \frac{d}{dx}(f(x)) = Df(x)$

1.  $(cf(x))' = cf'(x)$
2.  $(f(x) \pm g(x))' = f'(x) \pm g'(x)$
3.  $\frac{d}{dx}(fg) = fg' + gf' \quad \Rightarrow$  Product Rule
4.  $\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{gf' - fg'}{g^2} \quad \Rightarrow$  Quotient Rule
5.  $\frac{d}{dx}(f(g(x))) = f'(g(x))g'(x)$ , In Leibniz notation  $\frac{d}{dx}(y) = \frac{d}{du}(y) \times \frac{d}{dx}(u) \Rightarrow$  Chain Rule
6.  $\frac{d}{dx}(x^n) = nx^{n-1}$
7.  $\frac{d}{dx}(c) = 0$
8.  $\frac{d}{dx}(x) = 1$
9.  $\frac{d}{dx}(\sin x) = \cos x$
10.  $\frac{d}{dx}(\cos x) = -\sin x$
11.  $\frac{d}{dx}(\tan x) = \sec^2 x$
12.  $\frac{d}{dx}(\sec x) = \sec x \tan x$
13.  $\frac{d}{dx}(\csc x) = -\csc x \cot x$
14.  $\frac{d}{dx}(\cot x) = -\csc^2 x$
15.  $\frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}}$

$$16. \frac{d}{dx} (\cos^{-1} x) = \frac{-1}{\sqrt{1-x^2}}$$

$$17. \frac{d}{dx} (\tan^{-1} x) = \frac{1}{1+x^2}$$

$$18. \frac{d}{dx} (\csc^{-1} x) = \frac{-1}{x\sqrt{x^2-1}}$$

$$19. \frac{d}{dx} (\sec^{-1} x) = \frac{-1}{x\sqrt{x^2-1}}$$

$$20. \frac{d}{dx} (\cot^{-1} x) = \frac{-1}{1+x^2}$$

$$21. \frac{d}{dx} (e^x) = e^x$$

$$22. \frac{d}{dx} (\log x) = \frac{1}{x}$$

$$23. \frac{d}{dx} (a^x) = a^x \log a$$